

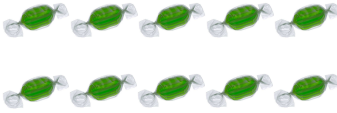
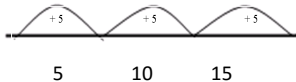
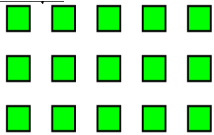
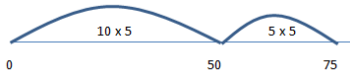


Progression in Calculation – Minimum Expectations in Multiplication

Year	Calculating	Counting & Mental Calculation
Minimum expectations by end of EYFS	<p>Jumping along number tracks/lines in steps of 1 and 2 using practical equipment.</p> <p>Grouping- counting in equal sized groups, e.g. coins, numicon, base 10 and socks.</p>  <p>1, 2, 3,..</p>	<p>Teacher recording if appropriate</p>
Y1	<p>Introduce the concept that multiplication is repeated addition.</p>  <p>= 10 + 10 + 10 = 3 x 10</p> <p>Pupils solve one-step problems involving multiplication by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher, e.g. I have 5 sweets and my friend has 5 sweets. How many sweets do we have altogether? 5 + 5 = 2 x 5</p>  <p>Using a 100 square to look at patterns of multiples of 2, 5 and 10, e.g. multiples of 5 end in 0 and 5.</p>	<p>Counting in 2, 5 and 10 from zero forwards and backwards.</p>
Y2	<p>Pupils calculate mathematical statements for multiplication and division within the multiplication tables and write them using the multiplication (x), division (÷) and equals (=) signs, e.g. 2 x 5 = 10 15 = 3 x 5</p> <p>Solve problems involving multiplication and division, using materials, arrays, repeated addition, mental methods, and multiplication and division facts, including problems in contexts, e.g.</p> <p>3 friends have 5 pencils each. How many pencils do they have altogether? <i>(repeated addition)</i></p>  <p>0 5 10 15</p> <p>This array can be described as:</p>  <p>5 x 3 = '5 multiplied by 3' or '5 times 3' or '5, three times' or 5 x 3</p> <p>To know that 2 x 3 is the same answer as 3 x 2 (commutativity) but 12 ÷ 3 is not the same as 3 ÷ 12.</p> <p>To explore problems such as: If you had the numbers 2, 5 and 10. How many different numbers sentences could you make? 2 x 5 =, 2 x 10 =, 5 x 10 =, 2 x 5 x 10 =</p>	<ul style="list-style-type: none"> Counting forwards and backwards in steps of 2, 5 and 10. <p><u>Mental Calculations</u></p> <ul style="list-style-type: none"> Practise and become fluent in the 2, 5 and 10 multiplication tables up to 12 x 2, 12 x 5, 12 x 10 and their related division facts

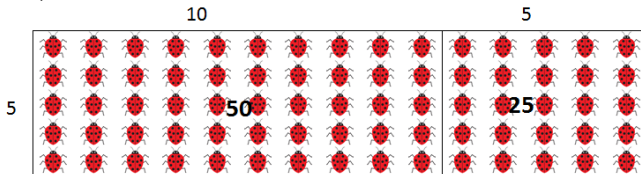
Y3

Build on their understanding of repeated addition and arrays to multiply two digits by one digit using tables they know, e.g. 15×5



Informal recording of partitioned numbers,
 $15 \times 5 = 10 \times 5 + 5 \times 5$

Link arrays to introduce grid multiplication to multiply HTU, e.g. 15×5 (up to $99 \times$)

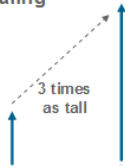


Use grid method to multiply HTU, progressing to formal written methods when appropriate (see year 4)

x	10	5	= 75
5	50	25	

$$15 \times 5 = \begin{array}{r} 10 \times 5 = 50 \\ 5 \times 5 = 25 \\ \hline 75 \end{array}$$

Scaling



Relate multiplication to scaling.
 My string is 12cm long. Cut a piece of string three times longer.

- Counting forwards and backwards in steps of 2, 3, 4, 5, 8, 10, 50, 100

Mental Calculations

- To know 2, 3, 4, 5, 8, 10 times tables up to $12 \times$ and their related division facts.

Y4

Pupils recap TU x U before moving to HTU x U and U x U x U using grid multiplication.

Multiplying by 0 and 1

Multiply two-digit and three-digit numbers by a one-digit number using grid multiplication progressing to expanded formal short multiplication. (short for multiplication of type TU x U or HTU x U)

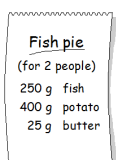
x	100	30	6	Grid Multiplication
5				

Leading to:

$$\begin{array}{r} 136 \\ \times 5 \\ \hline 30 \\ 150 \\ \hline 500 \\ \hline 680 \end{array} \quad \text{Expanded short multiplication}$$

Applying skills to word problems of the type:
 A bus has enough seats for 42 children. How many children could travel in 6 buses?

Scaling : recipes



Using simple scaling to solve problems, e.g.
 What ingredients would you need for 6 people?

- Counting forwards and backwards in steps of 6, 7, 9, 25, 100

Mental Calculations

- Know times tables up to 12×12 and their related division facts
- Factor pairs of a number, e.g. $12 = 1 \times 12, 2 \times 6, 3 \times 4$
- Using the associative law to make calculations easier, e.g. $2 \times 3 \times 4$ is the same as $2 \times 4 \times 3$

To be able to solve subtraction multiplication problems in contexts.

Y5

Multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication (*long for multiplication of type TU x TU or HTU x TU*).

Multiply ThHTU x U using an expanded short multiplication written method, e.g. 1345 x 6

```

1345
x  6
----
30
240
1800
6000
8070
    
```

Leading to:

```

1345
x  6
----
8070
2 23
    
```

Multiply TU x TU using the grid method, e.g. 38 x 72

x	30	8
70	2100	560
2	60	16

2160 576 2736

Progressing to:

```

      72
x   38
-----
    16 (2 X 8)
   560 (70 X 8)
   60 (2 X 30)
2100 (70 X 30)
  2736
    1
    
```

Application in word problems, e.g.

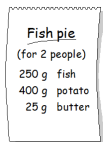
A shop sells DVDs for £2.50 each. What is the cost of 16 DVDs?

Scaling

Solve simple scaling problems, e.g.

If £1.00 = \$1.50, how many dollars would you get for £4.00?

How many mm are in 1.2 cm?

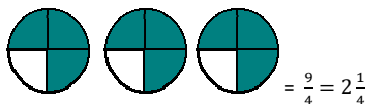


What ingredients would be needed for 7 people?

Multiplying proper fractions by a whole number, e.g.

$$\frac{3}{4} \times 3 = \frac{9}{4} = 2\frac{1}{4}$$

Pupils could use diagrams to support (linked to repeated addition)



To also multiply mixed numbers by whole numbers.

- Counting in $\frac{1}{2}$, $\frac{1}{4}$ etc

Mental Calculations

- Consolidate times tables up to 12 x 12 and their related division facts
- Know square numbers up to 144 (1, 4, 9, 16, 25, 36, 49, 64, 81, 100, 121, 144) with notation (2)
- Know prime numbers to 19 (2, 3, 5, 7, 11, 13, 17, 19)
- Know cube numbers up to 125 (1, 8, 27, 64, 125) with notation (3)
- To know and use the terms: factor, multiple and prime
- x by 10, 100, 1000 by moving the digits, including decimals
- Multiply numbers mentally using known facts, e.g. $25 \times 36 = 5 \times 5 \times 4 \times 9 = 100 \times 9$

Pupils multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of long multiplication.

124 × 26 becomes

$$\begin{array}{r} \\ 1 \ 2 \ 4 \\ \times \ 2 \ 6 \\ \hline 7 \ 4 \ 4 \\ 2 \ 4 \ 8 \ 0 \\ \hline 3 \ 2 \ 2 \ 4 \\ \end{array}$$

Answer: 3224

Y6

To multiply U.th x U, ThHTU x TU, HTU.t x TU

To multiply pairs of proper fractions and simplifying, e.g.

$$\frac{3}{8} \times \frac{2}{3} = \frac{6}{24} = \frac{1}{4}$$

Using an estimate to position the decimal point when dealing with decimals.

E.g. 3.24 x 4 ≈ 3 x 4

324

$\times 4$

1296

If the estimate is 12 then 3.24 x 4 = 12.96

Mental Calculations

- Find common factors multiples of a pair of numbers, e.g. the common multiple of 12 and 18
multiples of 12 are 12, 24, **36**, 48, 60, 72, ...
multiples of 18 are 18, **36**, ...
so common multiple is 36
- know prime numbers up to 30
- x numbers by 10, 100, 1000 involving decimals